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X-RAY EVALUATION OF CRYSTALS FOR STELLAR SPECTROMETERS

Nikos G. Alexandropoulos

Aerospace Corporation

Prepared for:

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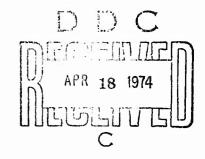
### X-RAY EVALUATION OF CRYSTALS FOR STELLAR SPECTROMETERS

Compiled by

N. G. Alexandropoulos Space Physics Laboratory

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#### FOREWORD

This report is published by The Aerospace Corporation, El Segundo, California, under Air Force Contract No. F0470-73-C-0074, and NASA Contract No. NAS8-27404.

Part I of this report, "Crystals for Stellar Spectrometers", is an original piece of work done by the author in collaboration with Dr. Gabrielle G. Cohen, Columbia Astrophysic Laboratory, Columbia University, New York, New York. Dr. Cohen's research was supported by NASA under Contract NAS5-11362.

Part II, "Crystal Diffraction Properties", was compiled by the author from the works of other investigators.

Part III, "Multi-Purpose Triple Crystal Spectrometer", presents some technical details of a spectrometer built by the author at Polytechnic Institute of Brooklyn.

This report, which documents research carried out from October 1972 through April 1973, was submitted on 27 February 1974 to Lieutenant Ernest L. Lockwood, DYAE, for review and approval.

Approved

G. A. Paulikas, Director Space Physics Laboratory

Publication of this report does not constitute Air Force approval of the report's findings or conclusions. It is published only for the exchange and stimulation of ideas.

Ernest L. Lockwood

1st Lt., United States Air Force

Project Officer

#### ABSTRACT

This report consists of three parts. The first part is an original piece of work done in collaboration with Dr. G. G. Cohen of Columbia University. It is an analysis of the principles involved in x-ray crystal evaluation and how they are applied to a number of crystals. The principles of crystal evaluation anlaysis as they apply to the special problems of x-ray astronomy are presented. A number of crystals were evaluated, and the energy dependence of the diffraction properties of (002) PET, (111) Ge, (101) ADP, (001) KAP, and (001) RAP are reported. The second part is a compilation of the diffraction properties of a number of crystals as reported by other authors. In the third part some technical details of a triple crystal spectrometer built by the author at Polytechnic Institute of Brooklyn are given. This spectrometer seems to be a most appropriate instrument for evaluation of crystal properties (%)

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#### INTRODUCTION

The need for compiled information on the diffraction properties of the crystals in designing an x-ray spectrometer is well appreciated by spectroscopists. However, only minor efforts have been made thus far in this direction, and a number of reports scattered throughout the literature are not easily available in an unified form to the designer. At the same time, a larger number of measurements performed by spectroscopists in their efforts to solve a specific problem never reach a publisher. The author's aim is to initiate the compilation of measured diffraction properties of crystals of some interest to the spectroscopist in a uniform way. He believes that it is possible to extend the present report to include previously unpublished data as well as furture measurements that are not extensive enough to meet the standards of an original publication but which can be very handy in eliminating duplication of effort. Perhaps now is the time to create a data bank where measurements will be reported in a standard format and will be made generally available.

#### PART I. CRYSTALS FOR STELLAR SPECTROMETERS

#### INTRODUCTION

Recent interest in x-ray astronomy has turned from energy dispersive x-ray spectrometer such as scintillation and proportional counters, in the study of stellar and solar spectra to wavelength dispersive instruments, the crystal spectrometers. The configuration of these spectrometers runs from the simple geometry of a single flat crystal spectrometer to the more complicated systems using x-ray collecting optics together with a crystal analyser. The basic ideas used in the new technology are not new to the field of x-ray spectroscopy and x-ray crystallography, but many of the special problems that arise in astrophysical spectroscopy are not easily solved in the usual ways. It is the purpose of this paper to present a review of crystal evaluation analysis as it applies to instrumentation employed in x-ray astronomy, and to offer some suggested solutions to the problems that are commonly encountered. The methods can easily be applied to future astronomical applications. A general approach for selecting the most appropriate crystals for a given problem will be given here, also. The detailed proofs for our analysis can be found in the references.

Designing a crystal x-ray spectrometer has been more of an art than a systematic procedure, in contrast to the methods commonly applied to designing other instruments. In addition, difficulties arise because there is no organized source of information about spectrometer components. Therefore, one usually cannot predict the performance of a given spectrometer without making extensive measurements.

The needs of the research define the requirements of the spectrometer to be built. Typical considerations are: (a) the spectral region to be covered, (b) resolution; (c) sensitivity; (d) reproductibility (e) accuracy; (f) linearity; (g) intensity to be measured; (h) the spectromete 's physical dimensions, weight, power needs, etc.; (i) scanning pattern; and (j) size of the source.

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Concerning the crystals to be used, the most pertinent information is the rocking curve as a function of energy, or at least the percent reflection (peak reflectivity), the rocking curve width at half maximum intensity and the coefficient of reflection (integral reflection coefficient). Other useful information includes: (a) the refractive index as a function of wavelength; (b) the crystal structure and the structure factor, |F|, for the specific reflections to be used; (c) the chemical stability and sensitivity to radiation damage; (d) the influence of surface treatment and corrosion on the diffraction properties; and (e) the mechanical properties of the crystal. Some of the above information can be found in the literature. Much more information is conveyed from investigator to investigator through private communications and never appears in print. For most crystals, the diffraction properties vary so widely with surface treatment that only actual crystal measurements are adequate.

Although studies of crystal perfection have become routine for several crystals, like silicon and germanium, for those wavelengths commonly used by crystallographers (.497°A - 2.29°A), considerable effort is needed in order to reach the same state of the art for the more complicated crystals and for the longer wavelengths of interest in x-ray astronomy.

#### CRYSTAL EVALUATION

After a tentative choice has been made as to the configuration of the spectrometer, the appropriate 2d spacing can be found from a diagram relating the spectral area to be covered to 2d. Such a diagram is shown in Fig. 1. We have assumed a single flat crystal configuration and have used the relation:

$$\lambda_{\min} \leq 2d \left(1 - \frac{4d^2 \delta}{\lambda^2}\right) \sin \theta \leq \lambda_{\max}$$
 (1)

where  $\theta_{min} \leq \theta \leq \theta_{max}$ .  $\theta_{min}$  and  $\theta_{max}$  are the specific angular limitations of the specific geometry,  $\delta$  is the deviation of the refractive index from unity.

The index to the powder diffraction file of ASTM <sup>(1)</sup> is a good starting point for preselecting a number of candidate crystals with a suitable 2d spacing. Some literature about these crystals can then be located from the same file. The crystal structure factor can be calculated using the extensive volumes Crystal Structures by Wyckof. <sup>(2)</sup> and the International Tables for Crystal Structure Analyses <sup>(3)</sup>, but such calculations are often hard to perform for interesting crystals. However, if only the point group is known, the multiplicity for a given reflection follows and relative values of |F| can be obtained from a powder pattern.

Before crystal diffraction measurements begin, some calculations as to optimum crystal performance can be made, as follows:

1) Dispersion, D.

$$D \equiv \frac{\delta \theta}{\delta \lambda} = \frac{1}{\lambda} \tan \theta \tag{2}$$

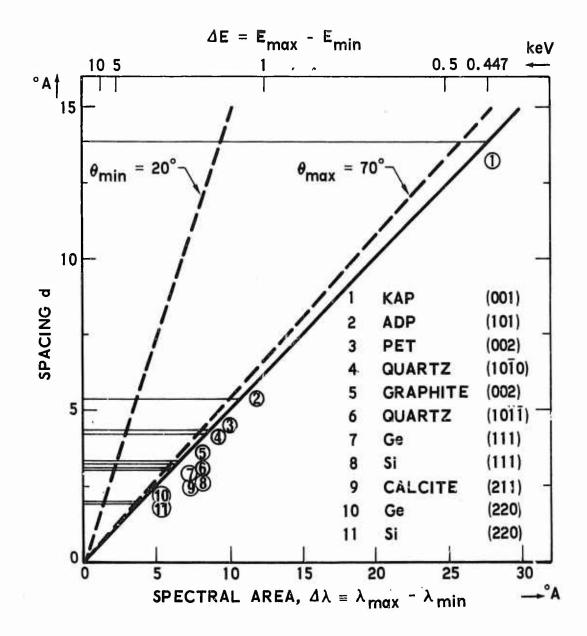


Figure 1. Spectral area in energy (upper scale) or in wavelength (bottom scale) covered by a single flat crystal spectrometer as a function of the crystal d spacing.

#### 2) Resolution, S.

$$S \equiv \frac{\lambda}{\delta \lambda} = \frac{E}{\delta E} = \frac{\lambda D}{W} = \frac{\tan \theta}{W}$$
 (3)

where W is the full width at half maximum (F.W.H.M.) of the recorded spectrum of a monoenergetic line and can be calculated from the crystal rocking curve, the collimator, and some geometrical factors. Let us call W<sub>c</sub> the crystal rocking curve full width at half maximum, W<sub>col</sub> the collimator angular divergence, and W<sub>mis</sub> other miscellaneous uncertainties involved in defining the Bragg angle  $\theta_B$ .

Although there is some disagreement about the correct relationship between W,  $W_c$ ,  $W_{col}$ , and  $W_{mis}$ , we prefer the relation used by Ehrenberg and Mark. (4) For the case of Gaussian distributions they give

$$W = \left(W_{c}^{2} + W_{col}^{2} + W_{mis}^{2}\right)^{1/2}$$
 (4)

#### a) Perfect Crystals

The FWHH =  $W_c$  (in radians) can be calculated, within the limits of Darwin's dynamical theory, from (5)

$$W_{c} = r_{o} \frac{N |F| (1 + |\cos 2\theta_{B}|)}{\pi \sin 2\theta_{B}} \lambda^{2}$$

$$= 1.79 \times 10^{-5} N |F| d^{2} (1 + |\cos 2\theta_{B}|) \tan \theta_{B}$$
 (5)

For  $W_c$  in seconds

$$W_C = 3.695 \text{ N} |F| d^2 (1 + |\cos 2\theta_B|) \tan \theta_B$$
 (6)

where d and  $\lambda$  are in Angstroms (Å), N is the number of unit cells Å  $^{-3}$ , |F| is the absolute value of the structure factor in electrons and  $r_0$  is the classified radius of the electron in Å. The solid line in figure 2 shows

$$\left\{\frac{W_c}{N|F|d^2}\right\}$$
 as a function of  $\theta_B$ .

For  $W_c$  in electron volts, Eq. (5) becomes

$$W_c = 1.112 \times 10^{-1} \text{ N} |F| d$$
 . 
$$\frac{(1 + |\cos 2\theta_B|)}{\sin \theta_B}$$
 (7)

The dashed line in figure 2 shows the quantity  $\left\{ \frac{W_c}{N \mid F \mid d} \right\}$ . It should be noted that this figure is general and applies to any crystal.

The other two components of equation (4), W<sub>col</sub> and W<sub>mis</sub>, to a first approximation, are independent of the incident radiation and their values can be larger or smaller then a given W<sub>c</sub>. In many astronomical applications W<sub>col</sub> is practically zero since the x-rays come from a "point source at infinity." W<sub>mis</sub> depends on the satellite stability and it is feasible to make W<sub>mis</sub> of the order of a few arc-seconds while W<sub>c</sub> can be in tens of minutes. In the case of laboratory measurements W<sub>mis</sub> is practically zero while with the slite it is feasible to achieve a W<sub>col</sub> of no more than a few seconds of arc.

For the sake of simplicity in deriving the spectrometer resolution, we suppose that

$$W_c^2 \gg W_{col}^2 + W_{mis}^2 \tag{8}$$

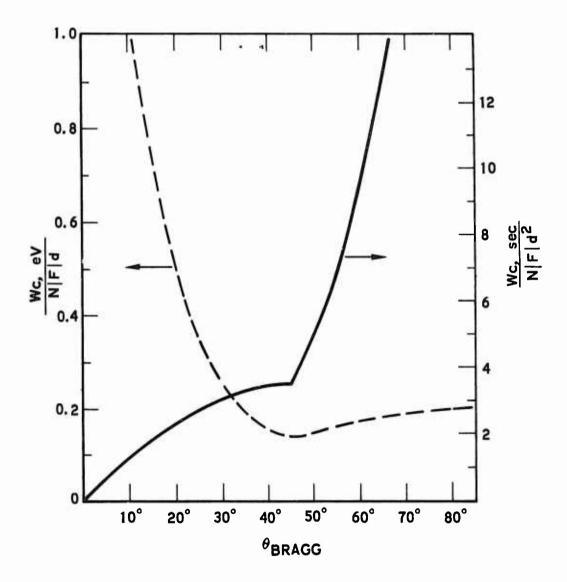


Figure 2. Normalized F.W.H.M. calculated according to Darwin's theory as a function of the Bragg angle. The solid line is in seconds (right scale) and the dashed line is in eV (left scale). This figure and figure 3 are applicable to any crystal.

In this case, the resolution can be calculated analytically and is given by

$$S = 5.574$$
 .  $\frac{10^4}{N|F|d^2}$  .  $\frac{1}{(1+|\cos 2\theta_B|)}$  (9)

Figure 3 shows S. N.  $|F| \cdot d^2$  as a function of  $\theta_B$ . When the approximation in equation (8) is dropped, then equation (9) is replaced by equation (3), and W is  $W_{tot}$ . It is important to note that the above discussion is largely a first-order approximation based on Darwin's theory, in which the peak reflectivity for a perfect crystal, independent of the crystal and the wavelength, is always set equal to unity. The integrated reflectivity is then proportional to  $W_c$ , being given by

$$R_{c} = \frac{8}{3\pi} r_{o} \frac{N \lambda^{2} |F|}{\sin 2 \theta_{B}} \left\{ \frac{1 + |\cos 2 \theta_{B}|}{2} \right\}$$
 (10)

It is more realistic to assume that some absorption can take place during diffraction. The peak reflectivity is then less than one, and the shape of the rocking curve is given by <sup>(6)</sup>.

$$F(\ell) = \frac{1}{2} \left[ \frac{(A+jB)/\delta}{\ell - j\frac{\beta}{\delta} \pm \left[ (\ell - j\frac{\beta}{\delta})^2 - (\frac{A+jB}{\delta})^2 \right]^{1/2}} \right]^2 + \frac{1}{2} \left[ \frac{\left|\cos 2\theta_B\right| (A+jB)/\delta}{\ell - j\frac{\beta}{\delta} \pm \left[ (\ell - j\frac{\beta}{\delta})^2 - (\frac{A+jB}{\delta})^2 \cos^2 2\theta_B \right]^{1/2}} \right]^2$$
(11)

where:

$$\ell = \frac{\sin 2 \theta_{\rm B}}{2 \delta} (\theta - \theta_{\rm B}) - 1,$$

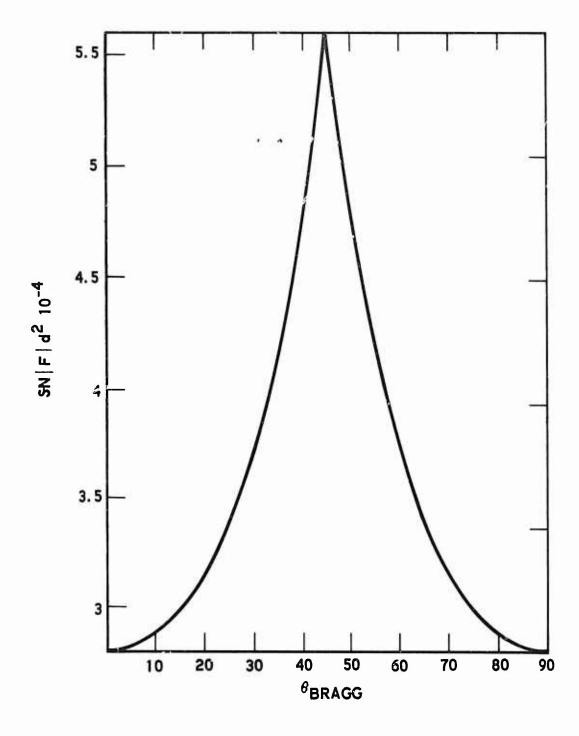


Figure 3. Normalized crystal resolving power as a function of  $\theta_{\mbox{\footnotesize Bragg}}$  (using Darwin's dynamical theory).

A and B are the real and imaginary parts of structure factor, F and  $\beta = (\lambda/4\pi)\mu\ell$ . (\$\mu\ell\$ is the linear absorption coefficient). Relation (11) is not valid near the x-ray absorption edges of the chemical compounds of which the crystal is made. The peak reflectivity can be calculated from equation (11) since it is equal to F(\$\ell\$\_0\$). Figure 4 is the diffraction pattern for (002) PET as calculated using another form of eq. (11) for \$\lambda = 8.34 A\$. In this particular case, the peak reflectivity is predicted to be F(\$\ell\$\_0\$) = .82.

When calculations such as those used to prepared Figure 4 cannot practically be carried out for several of the wavelengths that will be analyzed by the crystal, then some idea of the energy dependence of the peak reflectivity can be obtained by comparing the absorption coefficients near and far from the Bragg angle. When a photon strikes a crystal, photoelectric absorption, incoherent scattering, or coherenet scattering can take place. A measure of the incoherent scattering and the photoelectric absorption is the mass absorption coefficient  $\mu$ , which is energy dependent. Far from an absorption edge,  $\mu$  increases monotonically with  $\lambda^3$ , independent of direction. Near a Bragg reflection, attenuation can be described by an equivalent absorption parameter  $\tau$ .  $\tau$  can easily be calculated for the case of a perfect crystal and is given by

$$\tau = \frac{1}{2} r_0 N\lambda |F| , \qquad \tau >> \mu_{\ell}.$$
 (12)

The inverse of  $\tau$  or  $\mu$  determines the penetration depth. The penetration depth calculation predicts how much of the crystal will actually participate in each of the x-ray processes. When  $\tau \to \mu_{\ell}$ , the crystal is a poor reflector because a large proportion of the incident photons are absorbed by the crystal and re-emitted into  $4\pi$ , steradians, increasing the background. The crystal is then a poor analyzer crystal for this particular wavelength (7).

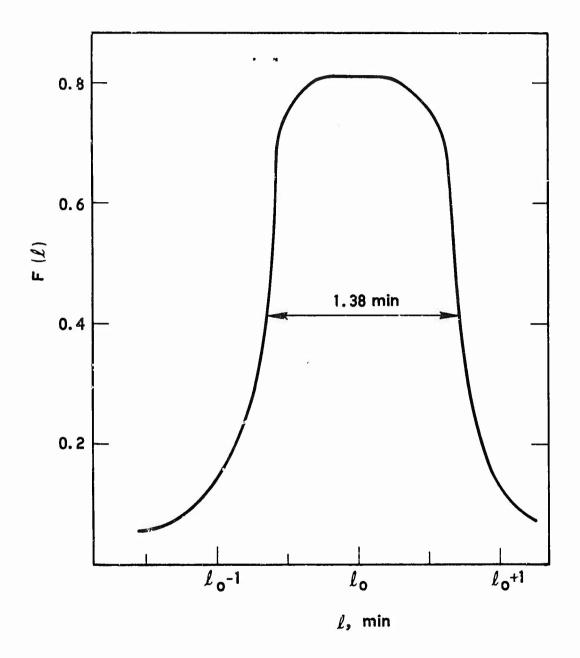


Figure 4. The theoretical rocking curve for a (002) PET crystal at  $\lambda$  = 8.34 Å.

#### b) Imperfect Crystals

The above analysis can be expected to hold to better than 1% when a spectrometer using perfect crystals is being designed. If imperfect crystals are chosen instead of perfect crystals, the only quantity that is well defined is the integrated reflectivity. The integrated reflectivity for an ideally imperfect crystal is given by (5).

$$R_{c}^{i} = \frac{1}{2\mu_{\ell}} r_{o}^{2} \frac{N^{2} \lambda^{3} |F|^{2}}{\sin 2\theta} \left[ \frac{1 + \cos^{2} 2\theta}{2} \right]$$
 (13)

This relation is derived by applying kinematical theory to a small single crystal (crystallite), and it is valid for the ideally imperfect crystal, where it is assumed that each crystallite diffracts independent of its neighboring crystallites. The intensity is proportional to the number of crystallites diffracting at any given time. Nevertheless, the measured integrated intensity is always less than that predicted by equation (13). The deviation between the measured and the calculated intensities increase with increasing |F | and increasing crystallite size. A measure of this deviation is given by the primary and secondary extinction. (8) When equation (13) is used in crystal structure work, crystallographers avoid measuring the 10 strongest lines. This indicates the limited use of equation (13) for x-ray spectrometers where, usually, only the strongest reflections are employed. There is no simple relationship between the shape of the ideally imperfect crystal diffraction pattern and the predicted integrated intensity. The .um, to a first approximation, depends only on the the critic ...cture and the mosaic spread.

The above discussion can lead to the misleading conclusion that the ideally imperfect crystal, unlike its perfect counterpart, will be adequately analyzed if measurements of the diffraction pattern are made at one wavelength. Actually, due to the strong dependence of the penetration depth on wavelength, and the dependence of crystal perfection on the distance to

the surface, it is still necessary to measure crystal properties for a sampling of wavelengths over the energy band for which the spectrometer will be used.

#### c) Extra Reflection

Regardless of the perfection of the crystals, for crystals used in broad band spectrometers, care must be taken with respect to the three dimensional orientation of the crystals to the incoming beam, in order to avoid asymmetrical Bragg reflections from planes not parallel to the crystal surface. (9) It is easy to identify higher order reflections from the planes (nh nk nl) when the planes (h k l) are parallel to the crystal surface. Indeed, the fact that higher order reflections occur may be very useful in identifying a questionable spectral feature that might otherwise be ignored. Higher order reflections are insensitive to a crystal rotation about the axis perpendicular to (h k l). On the other hand, asymmetrical Bragg reflections from planes making an angle with the (h k l) plane are difficult to identify, and are sensitive to the rotation mentioned above. This problem becomes more important in the single flat crystal geometry spectrometer when the detector is close to the crystal. The problem can be minimized by orienting the crystals so that reflections from planes other than (h k 1) do not reach the detector.

# MEASUREMENT OF THE DIFFRACTION PROPERTIES OF A CRYSTAL

Theoretical predictions give only a first order approximation of what can be expected from a given crystal. It is clearly necessary to proceed to experimental measurements in order to decide which mode will be most useful for a specific crystal, or which crystal will be most advantageous given a necessary mode of operation. In this section, the techniques for measuring crystal diffraction properties are described.

In principle, it is possible to measure the rocking curve of a crystal by measuring the diffraction pattern using any diffractometer, provided that the shape of the incident radiation is well known. Using the superposition theorem (10), the measured diffraction pattern  $\Phi(\theta)$  is the convolution of the incident beam (angular) profile  $\sigma(\phi)$ , the energy spread of the beam f(E), the actual crystal rocking curve F(L), and  $U(\phi, E)$  the apparatus profile. We can write

$$\Phi(\theta) = \sigma(\phi) \quad * \quad f(E) \quad * \quad F(\cancel{\ell}) \quad * \quad U(\phi, E) \tag{14}$$

where we wish to fine  $F(\ell)$ . The practical problems are in knowing f(E), which is nontrivial, and the accurate determination of  $\sigma(\phi)$  and  $U(\phi, E)$ . Assuming that all of these computations can and are made, the process is a very tedious one. In addition, the experimental error propagates very rapidly during a deconvolution calculation, necessitating very accurate experimental data in order to obtain marginal information about  $F(\ell)$ .

In a nondispersive system, the measured diffraction pattern is independent of the shape f(E), and  $U(\phi, E)$  i.e., the relation (14) reduces to

$$\Phi(\theta) = \sigma(\phi) \qquad * \qquad F(\mathbf{\ell}). \tag{15}$$

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If  $\sigma(\phi) = F(\ell)$ , the problem reduces to its simplest form, and the FWHM of the measured diffraction line  $\Phi(\ell)$  (assuming Gaussian shape) is  $\sqrt{2}$  times the FWHM for  $F(\ell)$ .

It is clear from the above that the only straightforward way to measure  $F(\ell)$  is through the use of a double crystal spectrometer in the parallel position, using two identical crystals. The reflection order should be the same for both crystals. This is the only nondispersive system, and only in this way does  $\sigma(\phi) = F(\ell)$ .

Although the best and simplest method of obtaining  $F(\ell)$  is through the use of a double crystal instrument in the nondispersive mode (1, -1), the actual measurements are very delicate, and special care (12) is necessary in data interpretation. The angle between s (the unit vector perpendicular to the crystal surface) and  $\vec{G}$  (the reciprocal lattice vector for the reflection planes) must be measured in advance, through one of the well-known crystallographic techniques, such as a back reflection Laue. If complicated corrections due to asymmetrical Bragg scattering and absorption are to be avoided, then the angle between  $\vec{s}$  and  $\vec{G}$  should be, to within a few seconds, equal to zero. The two crystals must be aligned so that  $\vec{k}_1$ ,  $\vec{k}_2$ ,  $\vec{k}_3$ ,  $\vec{G}_1$  and  $\vec{G}_2$  all lie in the same plane (see Fig. 5). If  $\vec{G}_2$  forms an angle with the  $\vec{k}_1$ ,  $\vec{k}_2$  plane,  $(\vec{k}_i = \frac{4\pi}{\lambda})$  sin  $\theta_i$ , the wave vector of the i beam) then the measured FWHM will be artifically widened. The detailed alignment of a double crystal spectrometer depends on the specific instrument, but some general discussion along these lines and a detailed analysis of the errors involved are given in the literature. (13-20)

In the present crystal study the double crystal vacuum spectrometer built by C. Howey and P. Metzger of the Space Physics Laboratory at The Aerospace Corporation was used. Most of the preliminary alignment is performed in air using a laser beam. The system consists of a 31.5-in diameter horizontal rotating table. The first crystal is supported by a model 10.553 Lansing mount on the axis of rotation. The incident x-ray beam  $\vec{k}_1$  is

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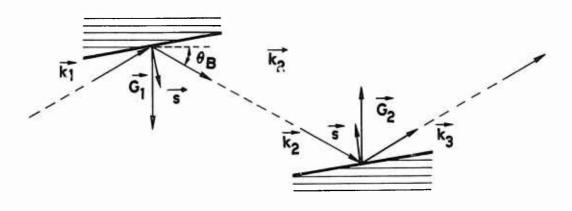


Figure 5. The alignment and orientation vectors characteristic to a double crystal spectrometer.

perpendicular to this axis. Using the table rotation around this vertical axis and the Lansing rotation about a horizontal axis, the  $\vec{k}_1$ ,  $\vec{k}_2$ , and  $\vec{G}_1$ vectors are brought into a horizontal plane (parallel to the plane of the table surface). On the same table, a second Lansing crystal mount can be made to slide in a precision motion along the table surface and perpendicular to the surface of the first crystal. The vector  $\vec{G}_2$  is then brought into the horizontal plane using the second crystal Lansing rotation around the horizontal axis. A flow proportional counter rotates around the vertical axis of the table and can also be made to spin about its own axis. The peak and the integrated reflectivity are measured by manipulating the counter so that it first sees the intensity diffracted from the first crystal and then measures the diffracted intensity from the second crystal. Using a lead screw, different parts of the second crystal surface are illuminated. Since different portions of the crystal are brought into the diffraction position, the system can be used for a Berg-Barrett topography study. During the alignment process, the intensity of the Bragg peak is measured as  $\vec{G}_2$  moves in a vertical plane. When  $\vec{G}_2$  approaches the plane of  $\vec{k}_1$ ,  $\vec{k}_2$ , and  $\vec{G}_1$ , the peak intensity increases sharply.

#### RESULTS

Applying the methods described above, the diffraction properties of several crystals of specific interest to x-ray astronomy were measured for a number of wavelengths. The measurements were carried out on: (002) PET, (111) Ge, (101) ADP, (001) KAP, and (001) RAP. A complete analysis has been carried out for the PET, as an example of the problems that are encountered in preparing crystals for a flight instrument. Diffraction results, however, are given for all the crystals tested, and are shown in the graphs which follow.

Pentaerythritol, or PET, is a tetragonal crystal with a bimolecular unit which has the dimensions:  $a_0 = 6.08 \text{ Å}$  and  $c_0 = 8.726 \text{ Å}$ . This is a body-centered grouping of C(CH2OH)4 molecules, in which each molecule consists of a tetrahedral distribution of (CH2OH) radicals about a central carbon atom. PET crystals were a popular crystal choice in the 1930's and 1940's because of their bending properties, large 2d, and the relative ease of growing large crystals. They frequently found application in bent crystal spectrometers, where their intense (002) reflection was used. They dropped from favor when it was learned that they are highly temperature sensitive and that they suffered radiation damage when they were exposed for long periods of time to a relatively intense x-ray beam. Recently there has been renewed interest in these crystals because the 2d spacing (8.73 A) has made them suitable for application to x-ray astronomy. Stellar and solar fluxes are expected to be weak enough so that the radiation damage properties of these crystals will not come into play under conditions commonly found in a satellite-borne spectrometer. PET, then, is a useful choice for a sample material on which to demonstrate the problems that are faced in crystal analysis for x-ray astronomy.

Figure 6 shows the FWHM for the best PET crystal available to us, as a function of angle (bottom scale), or as a function of x-ray energy (top scale). The scale on the right indicates the FWHM in arc minutes, while

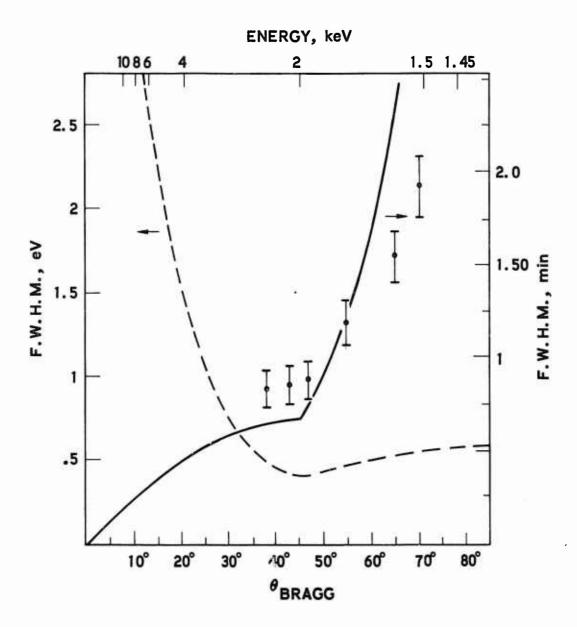


Figure 6. The measured F.W.H.M. $\sqrt{2}$ . Theoretical predictions are shown by the solid line in min (right scale) and by the dashed line in eV (left scale) as a function of the Bragg angle (bottom) or as a function of x-ray energy (top). The experimental data were taken using the best (002) PET crystal available to us.

that on the left is the same for eV. The points indicate our measurements, which were performed in arc minutes, and corrected assuming Gaussian distributions for the beam. (Actually, a line shape somewhere between Gaussian and Lorenzian is closer to the fact. Any correction assuming a distribution other than Gaussian will result in a narrower FWHM, so these measurements can be regarded as maximum measured values.) The solid line and dashed line indicate theoretical predictions using equations (6) and (7) respectively. The measured values are compared only to equation (6).

Data were taken for pentaerythritol crystals for as many as ten different incident wavelengths. Original crystals were tested as well as crystals that had been treated in the following ways: (1) heated and cooled from -30 to +50°C, (2) bonded with different vacuum grade urethanes, and (3) bonded and then subjected to controlled vibration tests simulating launch conditions. The crystal that was heated and cooled showed an increase in the FWHM at all the wavelengths tested. Figure 7 shows the results obtained from a crystal, such as that used to obtain the results shown in Figure 6, after it had been epoxied to a crystal mount with Solithane and vibrated according to a NASA Specification. The crystal appears to be under considerable stress after epoxying and vibration. In Figure 8 we show the FWHM in eV for these crystals in a spectrometer assuming different treatments and a mosaic spread of 1.5 minutes. The calculated (dashed line) and measured peak (solid line) reflectivities for our best PET crystal is shown in Figure 9.

In the ensuing figures, we show results for the FWHM and peak reflectivity of (111) Ge (Figures 10 and 11); the FWHM of (101) ADP (Figure 12); the FWHM of (001) KAP (Figure 13); and the FWHM of (001) RAP (Figure 14).

The observation reported earlier (24) on the influence of the crystal illumination on crystal diffraction properties has been verified again for ADP and extended to PET. When a beam of visible light from an incandescent lamp is focused on a ADP or PET crystal, the reflecting properties of the crystal change significantly. The changes of Bragg angle, FWHM and

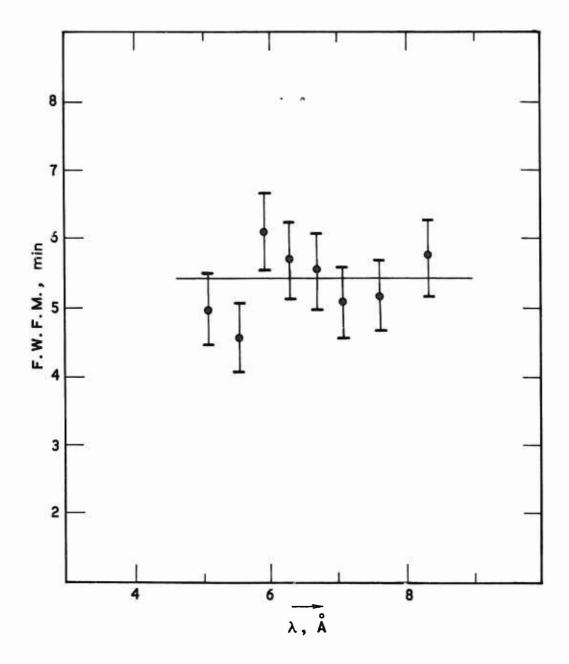


Figure 7. √2 (F.W.H.M.) obtained from a (002) PET crystal, similar to that used to obtain the results shown in Figure 6 after it had been bonded to a crystal mount with urethane and vibrated according to a NASA Specification.

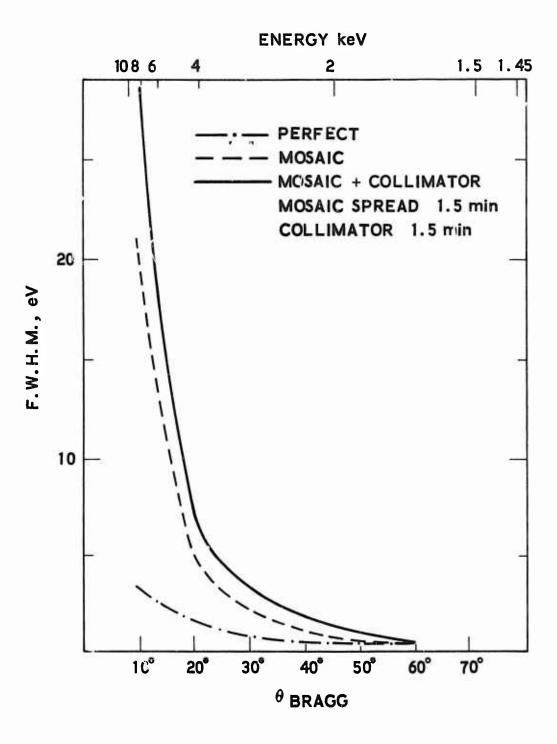


Figure 8. The F.W.H.M. for a perfect (002) PET crystal, a mosaic crystal with mosaic spread 1.5 min. and for a flat single crystal spectrometer using a mosaic PET crystal and a 1.5 min. collimator.

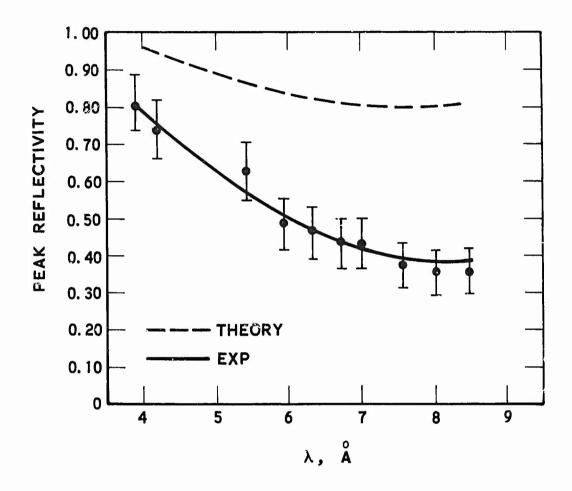


Figure 9. The calculated and the measured peak reflectivities for our best (002) PET crystal.

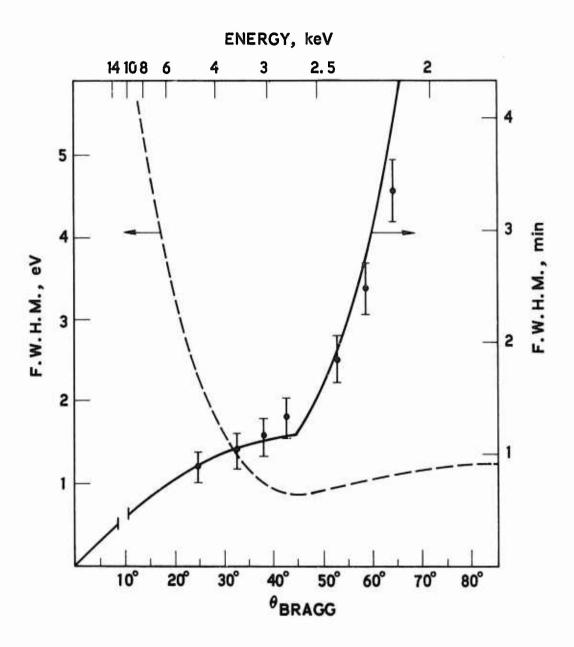


Figure 10.  $\sqrt{2} \times F.W.H.M.$  for a (111) Ge crystal.

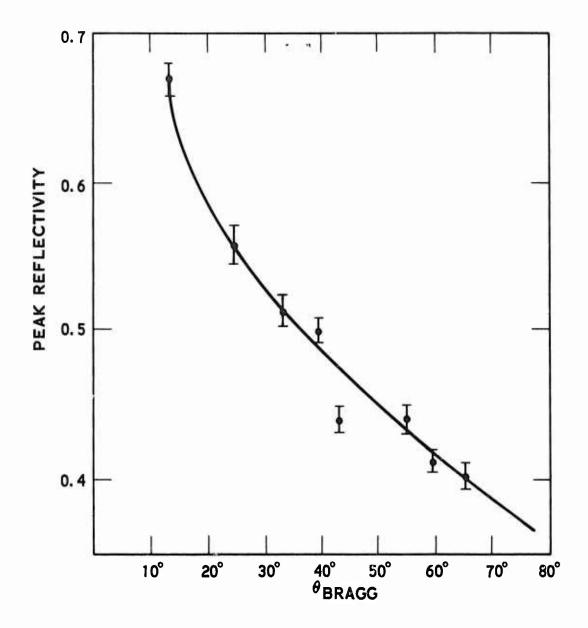


Figure 11. The measured peak reflectivity for a (111) Ge crystal.

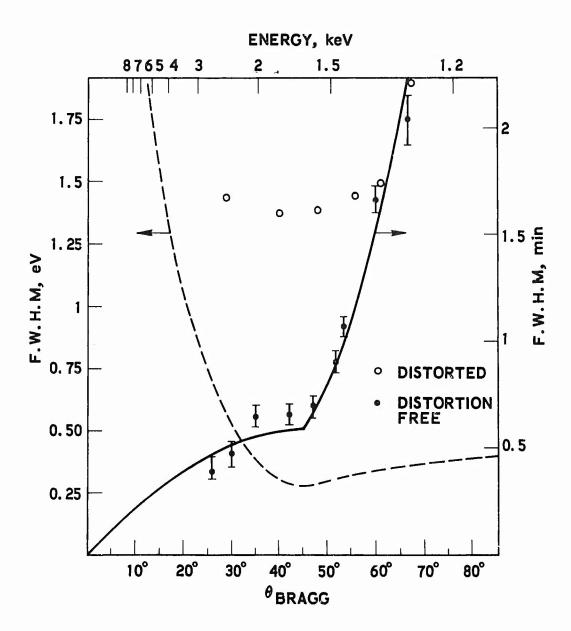


Figure 12. √2 × F.W.H.M. for a (101) ADP crystal. The solid circles are experimental data on the best ADP crystal available to us. The open circles are data on a distorted ADP crystal.

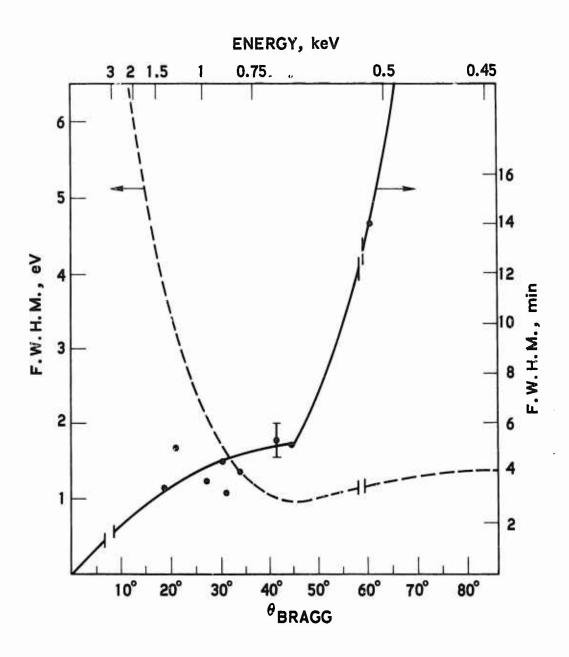


Figure 13.  $\sqrt{2} \times F$ . W.H.M. of a (001) KAP crystal. The short vertical lines indicate a deleted region near absorption edges where the theory is invalid.

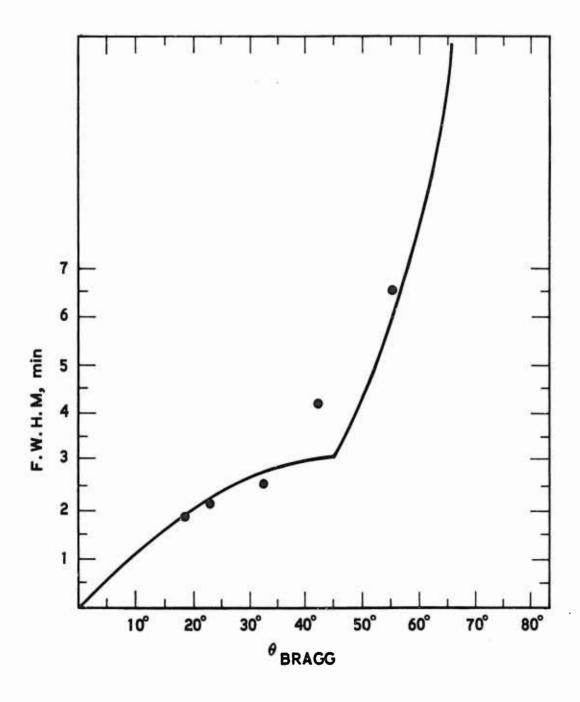


Figure 14.  $\sqrt{2} \times F.W.H.M.$  of a (001) RAP crystal.

peak reflectivity for an ADP crystal as a function of illumination time are shown in Figures 15, 16, and 17. The distortion of the crystal diffraction properties are not permanent and returned to their original values after the crystal was allowed to relax for several minutes with the light off.

Although this observation has not been quantitatively explained, it is clear as it is related to a local heating effect. We report it for the following reasons: (1) The observed changes (under laboratory conditions) in the diffracting properties of a crystal are significantly smaller than the changes that can occur during the observations in space; (2) the changes disturb the recorded x-ray spectra considerably because the line position and intensity depends upon the length of time that the line has been observed; (3) to dramatize the need for measuring the crystal diffraction properties under actual flight conditions or in an in-flight calibration.

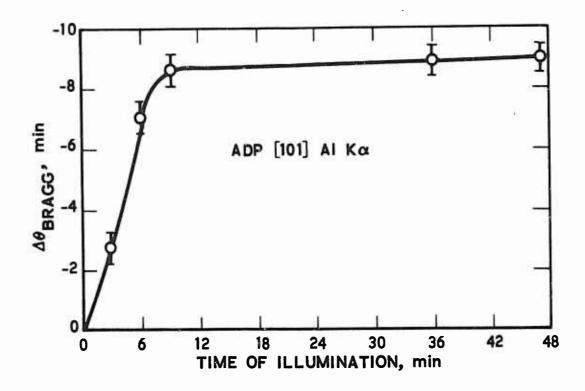


Figure 15. Sift of the Bragg angle of Al  $K\alpha$  radiation scattered by a (101) ADP crystal as a function of the crystal illumination by an incandescent lamp.

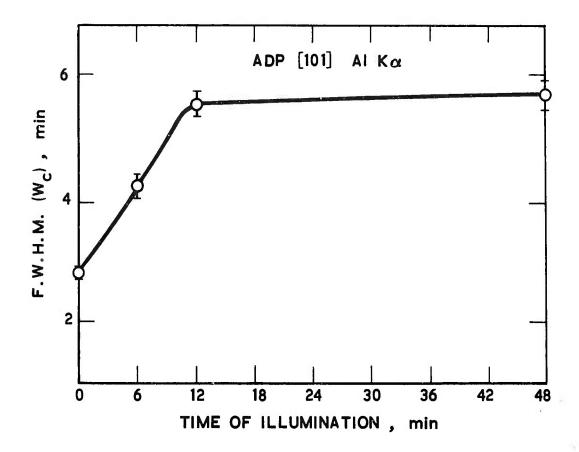


Figure 16. F.W.H.M. as a function of the illumination time for a (101) ADP crystal.

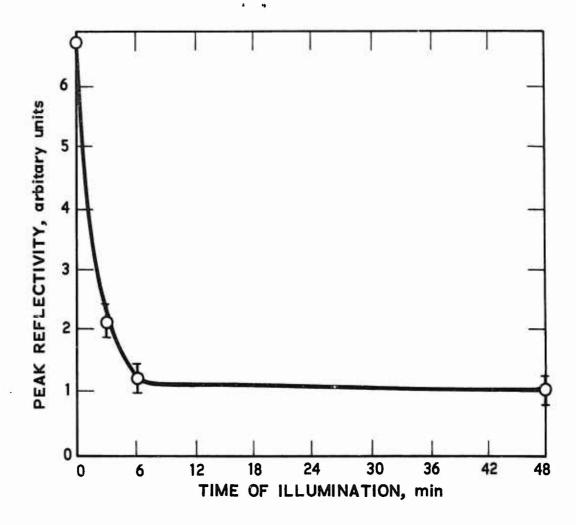


Figure 17. The peak reflectivity for a (101) ADP crystal as a function of the illumination time.

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- 6. G. Brogren, Arkiv for Fysik, 6, 321-334 (1953).
- 7. In addition, it may be necessary to calculate that contribution to the total mass absorption coefficient arising from crystal impurities with absorption edges in the vicinity of the spectral region that will be under investigation.
- 8. A mosaic crystal is said to be ideally mosaic if primary as well as secondary extinction is negligibly small for all reflections. This condition is much more easily satisfied for weak than for strong reflections. Thus a crystal may be "ideally mosaic" only for its weak reflections.
- 9. N. Spielberg and T. Labell, J. Appl. Phys. 31, 1659-1664 (1960).
- 10. N. G. Alexandropoulos, Phys. Rev. <u>150</u>, 610-613 (1966).
- 11. It is necessary to take the same order reflection from both crystals of the double crystal spectrometer because it is obvious from Eq. 5 that  $W_{\rm C}(\lambda_1)=W_{\rm C}(n\lambda_0)$  for  $1=n_0$ . In making precision measurements, special care is taken not to excite  $\lambda_0$ . An arrangement using different crystals or different reflection order would be appropriate for topography or for unique defect imaging. It has sometimes been attempted to perform rocking curve measurements using two different crystals in a double crystal spectrometer. (Here we are discussing crystals of different 2d). In this case the dispersion of a double crystal spectrometer in the parallel mode is given by

$$D = \frac{{}^{n}A}{2d_{A}\cos\theta_{A}} - \frac{{}^{n}B}{2d_{B}\cos\theta_{B}}$$

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where  $n_A$  and  $n_B$  are the reflection orders of the first and second crystals, respectively. If two different crystals are used, one might still, somehow, be able to choose the 2d spacing and the reflection orders so that the above equation goes to zero. However, if  $D \neq O$ , the resulting rocking curve will have to be corrected by deconvolution.

- A. H. Compton, S. K. Allison, X-rays in Theory and Experiment (Van Nostrand Co., Inc., New York, 1935).
- Suppose that, by some undesirable circumstance the crystal for which 12. we wish to make rocking curve measurements is a piece of polycrystalline silicon, and it was assumed that the crystal is (111) single crystal silicon. If, for simplicity, we neglect absorption, this crystal is equivalent to a mosaic crystal with mosaic spread of 360 degrees, or to a (111) thin Si crystal that has been bent (uniformly stressed) into a cylinder. Let us determine the rocking curve of this Si sample using a well-collimated monochromatic incident beam (coming off a perfect flat Si crystal) and a stationary detector. The measured FWHM of this crystal is then 360°, because independent of the angle between the surface and the beam some part of the sample is always reflecting. We now replace the stationary detector with a detector that is rotating accurately in a  $\theta$  -  $2\theta$  motion. If the acceptance angle of this detector is of the same order as the divergence of the incident beam, and smaller than the rocking curve width of a perfect Si (111) crystal, then the measured FWHM of the cylindrical silicon (111) crystal is dependent only on the diffraction properties of a single stressed crystal domain. Going now to a flat crystal, it is clear from the above example that when stationary detectors with large acceptance angles are used, even with a well-collimated incident beam, the diffraction width that will be seen is that of the entire crystal. If the crystal is perfect, the width will be much narrower than that which will be seen for a similar crystal in its imperfect form. The above ideas are summarized in the following table.

Crystal	Detector	FWHM	Resolution S
Polycrystalline or cylinder	stationary collimated	360°	0
	rotating collimated	x sec	3000
	stationary large accept	x < y < 360°	<3000
	rotating large accept	x < y < 360°	<3000
Single flat	rotating large accept	x sec	~3000

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## PART II. CRYSTAL DIFFRACTION PROPERTIES

This second part of this report is composed of crystal diffraction properties for a number of crystals measured by other investigators. The FWHM is given in arc-minutes and in eV. For most of the crystals, the values expressed in eV were derived by converting the measured values of FWHM in arc-minutes or arc-seconds and not from direct measurements. In the absence of reported values for the integrated reflectivity, its value can be easily calculated assuming a Gaussian shape for the rocking curve with the known width and height. The table preceding the graphs is a summary of information coming from these graphs in addition to those collected from other sources.

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Table I. Properties of Crystals Frequently Used in X-ray Spectroscopy

				GENERAL INFORMATION	IATION			
No.	Ref.	Crystal	Chemical Composition	Crystal Structure	Lattice Parameters	Perfection	Stability	Mechanical Properties
	4 0 6	Potassium acid Phthalate KAP	кнс <sub>6</sub> н <sub>4</sub> (соо) <sub>2</sub>	Orthorhombic (tetramolecular cell)	a = 6.466 # b = 9.609 c = 13.857	Fair	Fair	Soft, easily cleaved
2	1	Rubidium acid Phthalate RAP	RbHC <sub>6</sub> H <sub>4</sub> (COC) <sub>2</sub>	Orthorhombic	a = 6.55 b = 10.02 c = 13.06	Fair	Fair	Soft
ю	4	β Alumina	NaA11017	Hexagonal (unimolecular cell)	a = 5.595 c = 22.49	Almost Perfect	Good	Hard, brittle
4	4 v	Mica (Muscovite)	KA![A! <sub>2</sub> Si <sub>3</sub> O <sub>10</sub> ] [OH] <sub>2</sub>	Monoclinic	a = 5.19 b = 9.03 c = 20 β = 95.77°	Almost Perfect	Perfect	Easily cleaved, bent
ĸ	4.0	Gypsum	CaSO <sub>4</sub> · 2:120	Monoclinic	a = 10.47 b = 15.15 c = 6.5 ß = 151.51°	Fair	Poor	Soft
9	41	8 Alumina	NaA <sup>1</sup> 11 <sup>0</sup> 17	Hexagonal (unimolecular cell)	a = 5.95 c = 22.49	Almost Perfect	Good	Hard, brittle
7	7	Ammonium dihydrogen phosphate ADP	NH <sub>4</sub> H <sub>2</sub> PO <sub>4</sub>	Tetragonal (tetramolecular cell)	a = 7.510 c = 7.564	Good	Fair	Soft
ω	9	Ethylene diamine-D- tartraté EDdT	C <sub>6</sub> H <sub>14</sub> N <sub>2</sub> O <sub>6</sub>	Monoclinic	a = 8.97 b = 8.808 c = 5.959 β = 105.51°	Fair	Poor	Soft
6	194	Pentaerytritol PET	С(СН <sub>2</sub> ОН) <sub>4</sub>	Tetragonal (bimolecular cell)	a = 6.083 c = 8.726	Good	Poor	Soft, easily cleaved

\* b, c, in A as given by R. W. G.  $\text{Wyckoff}^{\{16\}}$  #The values given by A. T. Bearden et al  $^{(17)}$  are a = 6.47, b = 9.62, C = 13.3164

Table I. Properties of Crystals Frequently Used in X-ray Spectroscopy (Continued)

	Mechanical Properties	Hard. Can be bent	Hard. Can be bent	Soft, brittle	, Hard	Hard. Can be bent	Hard	Hard. Can be bent	Easily cleaved, bent	Hard
	Stability	Perfect	Perfect	Fair	Good	Perfect	Good	Perfect	Perfect	Good
	Perfection	Perfect	Perfect	Very Poor	Fair	Perfect	Good	Perfect	Almost Perfect	Fair
FORMATION	Lattice Parameters	a = 4.913 c = 5.405	a = 4.913 c = 5.405	a = 2.456 c = 6.696	a = 6.60	a = 5.6575	a = 5,451	a = 5.43808	a = 4.989 c = 17.026	a = 5.64
GENERAL INFORMATION	Crystal Structure	Hexagonal centrosymmetric	Hexagonal centrosymmetric	Hexagonal	Cubic	Cubic	Cubic	Cubic	Hexagonal	Cubic
	Chemical Composition	SiO <sub>2</sub>	SiO <sub>2</sub>	C	KBr	Ge	CaF <sub>2</sub>	Si	CaCO <sub>3</sub>	NaCl
	Crystal	a Quartz	a Quartz	Graphite	Potassium bromide	Germanium	Calcium fluoride (Fluorite)	Silicon	Calcium carbonate (calcite)	Rock Salt
	Ref.	5,8 9 10	46	11	4	1 12	4.02	6 13	8 5 14	41 A D
	No.	10.	11	12	13	14	15	16	1.7	18

\*a, b, c, in A (Ref. 16)

Table I. Properties of Crystals Frequently Used in X-ray Spectroscopy (Continued)

				GENERAL IN	GENERAL INFORMATION			
No.	Ref.	Crystal	Chemical Composition	Crystal Structure	Lattice Parameters	Perfection	Stability	Mechanical Properties
19	8 10 15	a Quartz	sio <sub>2</sub>	Hexagonal centrosymmetric	a = 4.913 c = 5.405	Perfect	Perfect	Hard. Can be bent
20	5	Aluminum	Al	Cubic	a = 4,049	Alme.t Perfect	Good	Soft
21	'n	Topaz (AlSilicate)	AL <sub>2</sub> S <sub>1</sub> O <sub>4</sub> (E, OH) <sub>2</sub>	Orthorhombic	a = 4.64 b = 8.78 c = 8.37	Good	Good	Soft
22	2	a Quartz	SiO <sub>2</sub>	Hexagonal centrosymmetric	a = 4.913 c = 5.405	Perfect	Perfect	Hard. Can be bent
23	4,5 6 11	Lithium fluoride	LiF	Cubic	a = 4.028	Almost Perfect	Perfect	Hard, plastically bent
24	12	Germanium						
52	5	Fluorite						
97	13	Silicon						
22	14	Calcite						

\* a, b, c, in A (Ref. 16)

Table I. Properties of Crystals Frequently Used in X-ray Spectroscopy (Continued)

	Fig.		13	14	<b>A</b>	1	4	1	12	4	9 6
	Rc105rad at 9B 1	Min. Max.	7.5 17.5 7.46° 57.22°	ilable					Not Available		Not Available
	-%	Max.	7.46	Not Available	le	lle .	le •	le		-ie	.80
	B Pat 0B	2	.01		Not Available	Not Available	Not Available	Not Available	51.50°	Not Available	.38
	*Sat 0BT	Max.	1380 45°	1780 33°	Ž	ž	ž 	ž 	10460 45°	N 	7640 45°
	F.W.H.M at 0	Max.	9.91	4.64					1.46'		1.30'
ERTIES	F.W.H	Min.	2.26' 18.5°	1.31				V	. 27'		37.96
DIFFRACTION PROPERTIES	E(keV)**	Max.	2.577	2.738	3.176	3.59	4.708	6.353	6,699	8.107	8.180
FRACTIC	E(ke	Min.	.454	.482	.560	. 633	.830	1.120	1.180	1.429	1.445
DIF	Spacing	Zd, A	27.714#	26.12	22.49	19.884	15.168	11.24	10.659	8.808	8.726
		Reflection	001	001	2000	005	220،	₽0:00	101	020	005
		Crystal	Potassium acid Phthalate (KAP)	Pubidium acid Phthalate (RAP)	β Alumina	Mica (Muscovite)	Gypsum	β Alumina	Ammonium dihydrogen phosphate ADP	Ethylene diamine-D- tartrate EDdT	Pentaerytritol PET
		Ref.	- N E	-	4	5	4	4	7	9	1 9 4
		oN	-	7	3	4	5	9	7	8	6

The value given in Ref. 17 is 2d = 26.633 A

Table I. Properties of Crystals Frequently Used in X-ray Spectroscopy (Continued)

				Û	IFFRAC	TION PRO	DIFFRACTION PROPERTIES							
Ref. Crystal Reflection		Refle	ction	Spacing 2d, A	** min	*** max	**** min	max	max	11 min	max	ttt min	††† max	Fig.
5,8 \(\alpha\) Quartz \(10\overline{10}\) 9 10		101	<u>0</u>	8.512	1.485	8,423	.032'	971.	20500 52.69°	.065	7.29	1.04	11 70.99	19 20
4 α Quartz 1011		101	F	6.7153	1.89	10.72	.046'	1.32'	11100	71.55°	.79	1.6 4.8°	13.9	21
11 Graphite 002		005		969.9	1.879	10.75	41.4'	87' 30.1°	~300		Not /	Not Available		1
4 Potassium 200 bromide	E	200		09.9	1.91	10.85	V		No.	Not Available	e			1
1 Germanium 111		111		6.5327	1.927	10.93	0.91'	3,35¹ 65	6100 43°	0.40 65°	. 67.			10 14
4 Fluorite 111 6 5		111		6.28	2.049	11.37	V		No.	Not Available	9			
6 Silicon 1111		111		6.271	2.078	11.39	0.072' 6.4°	. 62'	11000 23.30°	.43	11.72°	2 6.4°	10.3 14.17°	23 24
8 Calcium 211 5 carbonate 14 (calcite)		211		690.9	2.084	11.799	.06151	1.5217	15400 18.30°	.43	.73	2.4 6.72°	30.3	25/26
4 Rock Salt 200 6 5		200		5.64	2.23	12.66	V		No.	Not Available				1

Table I. Properties of Crystals Frequently Used in X-ray Spectroscopy (Continued)

	17 90	25- 32-	4	1	1	1	3.3	4	35	26 28
	Rcmax	3.2 <del>4</del> 69.35					23.4		6.0a 51.55°	.91
	Rc min	55 6.53°					1.7		.89	.37
	P max	18,22	able —	able	able	able *	. 68	able —	. 68	.491
	11 Prain	.17	Not Available	Not Available	Not Available	Not Available -	.42	Not Available	.49	. 24' 64.97°
	S <sub>max</sub>	31200			1		12800 16.15		29200 30.3	63946 30.5
	**** W	.461					.8361		.23' 51.55°	0.65'
TIES	**** W	.038'		V			. 0731		.038'	13.53
DIFFRACTION PROPERTIES	*** E keV	14.537	15.323	15,393	16.818	17.76	17.85	18.59	18.59	23.536
FFRACTIC	** Eminkev	2.563	2.70	2.715	2.96	3.132	3.147	3.279	3.279	4.15
ī	Spacing 2d, A	4.912	4.66	4.638	4.246	4.028	4.00	3.84	3.8399	3.034
	Reflection	1120	111	200	2020	200	220	022	220	422
	Crystal	a Quartz	Aluminum	Topaz (Al Silicate)	a Quartz	Lithium fluoride	Germanium	Fluorite	Silicon	Calcite
	Ref.	8 10 15	rv 4	ທ	c.	4,5 6 11	12	r.	13	14
	No.	19	20	21	22	23	24	25	97	27

Table I. Properties of Crystals Frequently Used in X-ray Spectroscopy (Continued)

	ig	1	38	1	<b>A</b>	39	26
	Rc III Fig.		.91			38.97 4	. 63 2
	Rc !!!		.31			.19	.34
	p ††	able	34.07	able	able	.61	20.54
	Pmin	Not Available	.52	Not Available	Not Available	.58 38.97°	.48
	**** S T		87173 34.07			. 018' 144 000 8. 97° 32. 22	.033'122000 49.56° 49.56°
	**** W max		.471			33	.033
ERTIES	**************************************	V	.017'			.00831	.018'
DIFFRACTION PROPERTIES	*** E keV	25.07	25.45	26.331	29,134	35, 28	35,35
DIFFRACT	## *** Emin keV Emax keV	4.421	4.487	4.643	5.137	6.221	6.233
	Spacing 2d, A	2.848	2.806	2.712	2.451	2.024	2.02
	Reflection	220	2023	303	2240	2243	633
	Crystal	Lithium fluoride	a Quartz	Topaz	a Quartz	ø Quartz	Calcite
	Ref.	9	4 &	6 15	9	œ	# #
	Š.	82	29	30	31	32	33

\*\* The value of the minimum (maximum) energy, assuming maximum (minimum) feasible Bragg angle 80° (10°).

 $\ast^{\dagger}$  The reported value of the FWHM in minutes (top); the Bragg angle  $\theta_{B}$  at which the FWHM has been measured (bottom).

The resolution of a double crystal spectrometer S (E/ $\Delta$ E) (top);  $\theta_{\rm B}$  (bottom).

f\* The peak reflectivity P (top); B (bottom).

The integrated reflectivity  $R_c$  in  $10^{-5}$  radians (top);  $\theta_B$  (bottom).

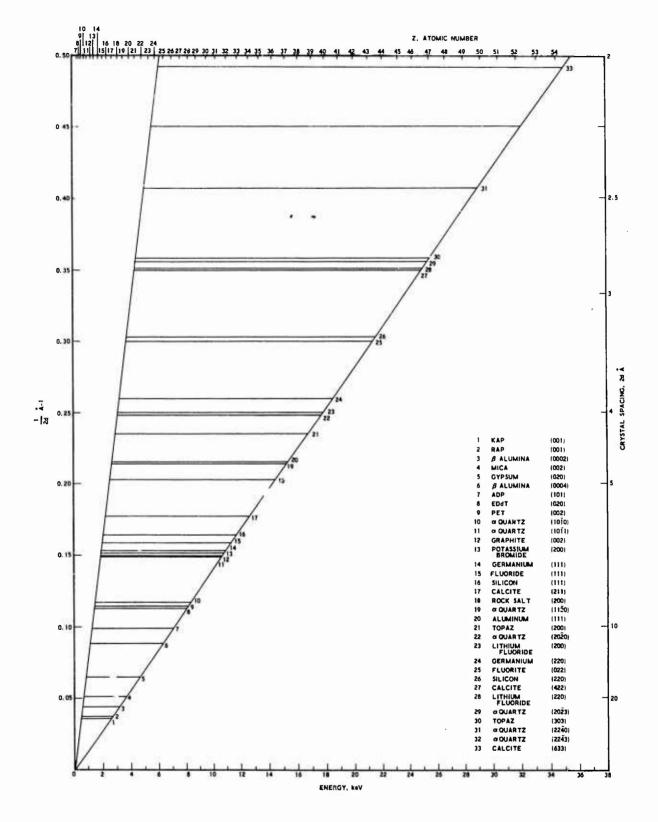


Figure 18. Spectral region in energy (bottom scale) or in elements K-absorption edge (top scale) covered by a single flat crystal spectrometer as a function of 2d spacing for a number of crystals.

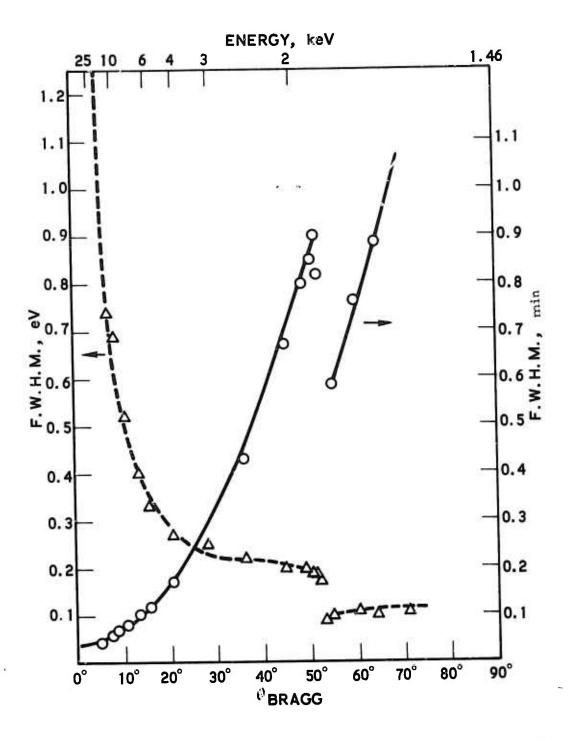


Figure 19. T.W.H.M. of (1010) quartz. Solid line in minute x√2 (right-hand scale), dashed line in eV (left-hand scale) as a function of the Bragg angle (bottom) or as a function of x-ray energy (top). The experimental data are reported by G. Brogren (9).

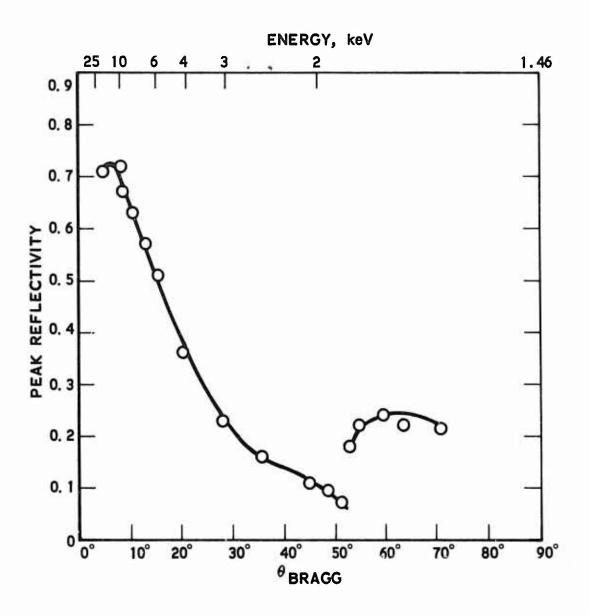


Figure 20. The peak reflectivity of (1010) quartz as a function of the Bragg angle (bottom) or as a function of x-ray energy (top). The experimental data are reported by G. Brogren. (9)

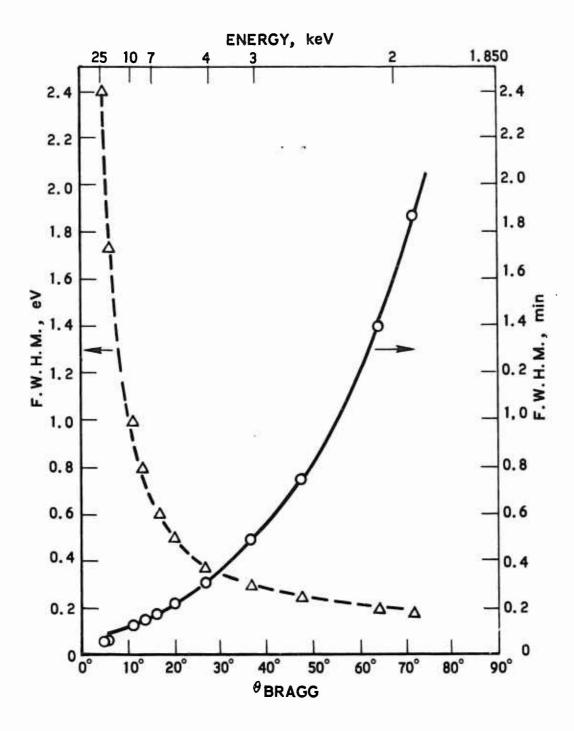


Figure 21.  $\sqrt{2} \times F.W.H.M.$  of (1011) quartz. The experimental data are reported by G. Brogren(9).

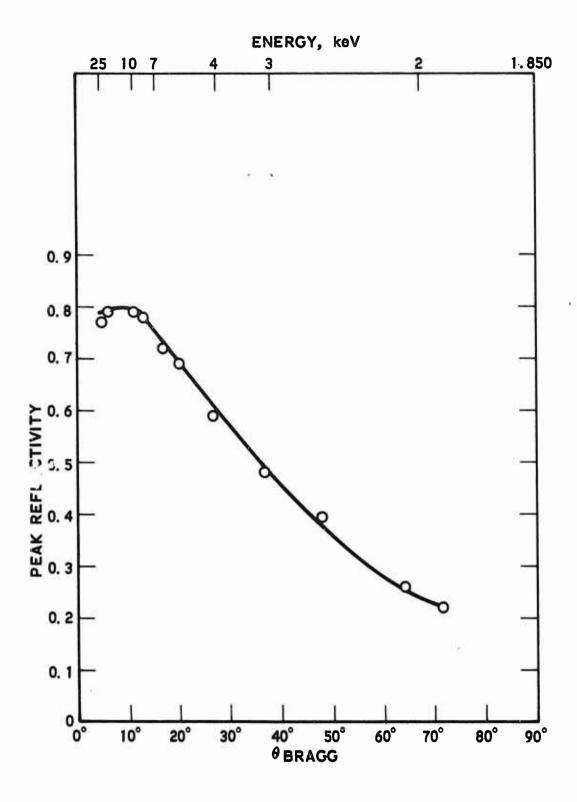


Figure 22. The peak reflectivity of (1011) quartz. The experimental data are reported by G. Brogren (9).

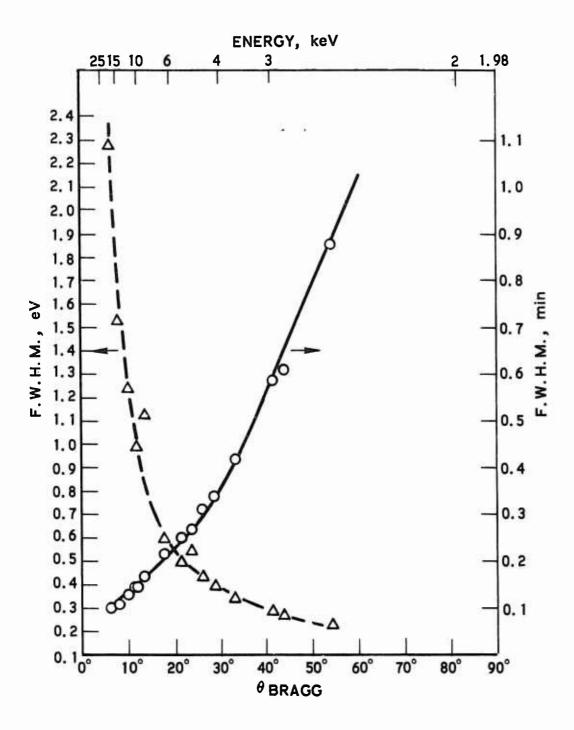


Figure 23.  $\sqrt{2} \times F$ . W.H.M. of (111) silicon. The experimental data are reported by Brogren (13).

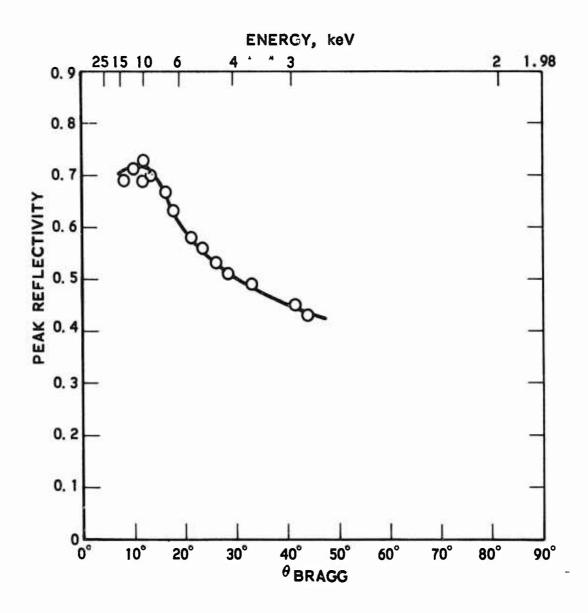


Figure 24. The peak reflectivity of (111) silicon. The experimental data are reported by Brogren et al (13).

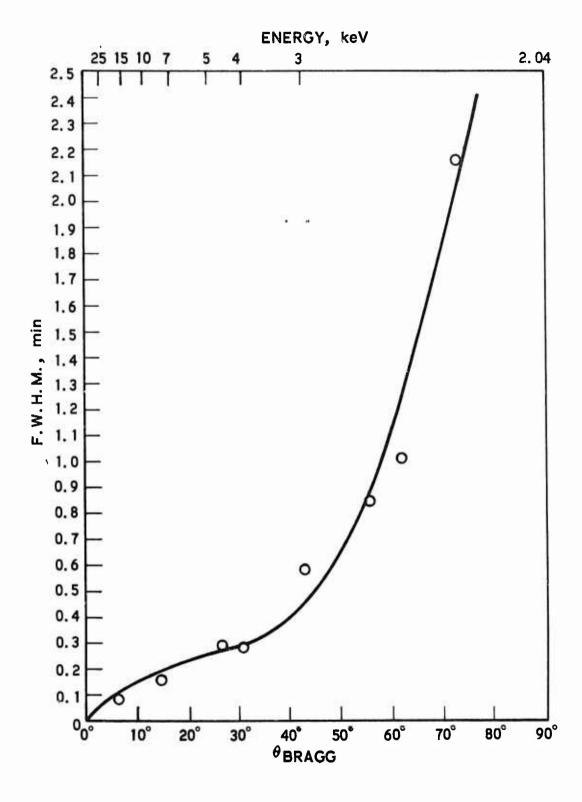


Figure 25.  $\sqrt{2} \times F$ . W.H.M. of (211) calcite in minutes as a function of the Bragg angle (bottom scale) or as a function of the x-ray energy (top) scale. The experimental data are reported by Paratt et al<sup>(14)</sup>.

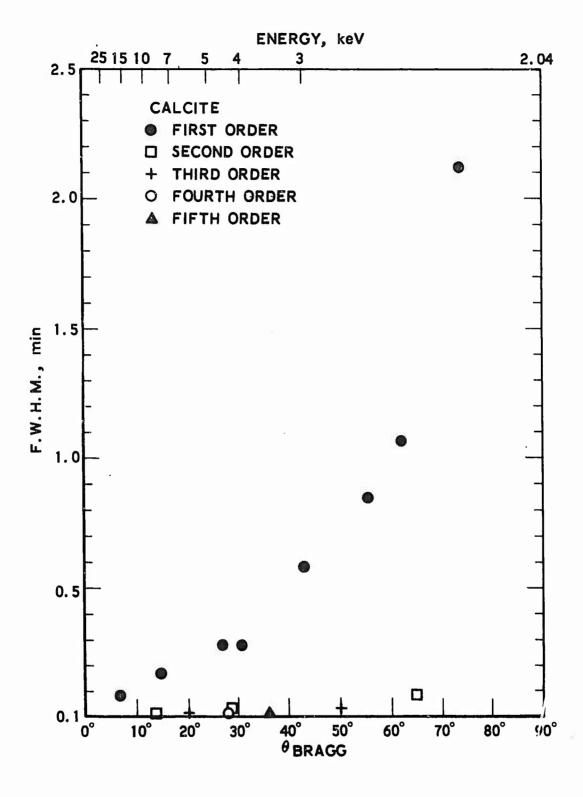


Figure 26. √2 × F.W.H.M. for calcite (211) at first, second, third, fourth and fifth order of reflection. Notice the decrease in intensity with the increase of the reflection order. Data reported by Parrat et al<sup>(14)</sup>.

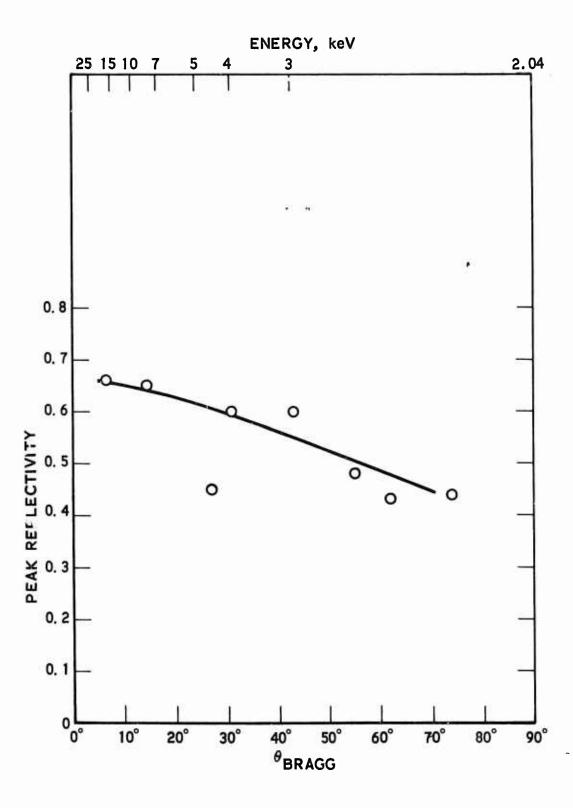


Figure 27. The peak reflectivity of (211) calcite. Data reported by Paratt et al<sup>(14)</sup>.

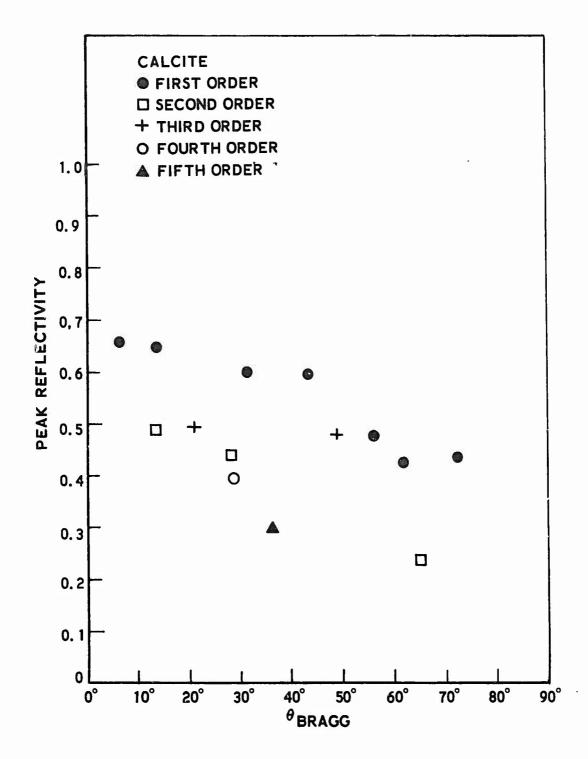


Figure 28. The peak reflectivity of (211) calcite for a number of reflection. Data reported by Paratt et al (14).

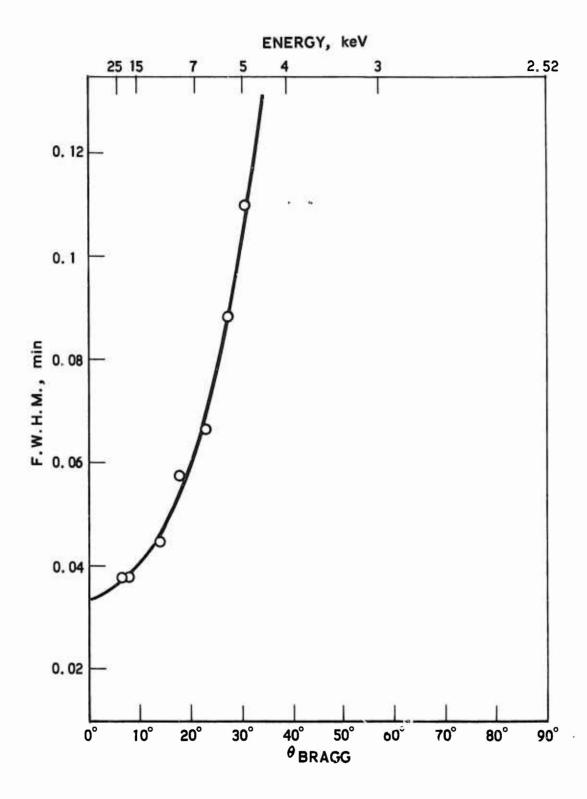


Figure 29. The F.W.H.M. of (1120) quartz. Data are reported by Brogren(10).

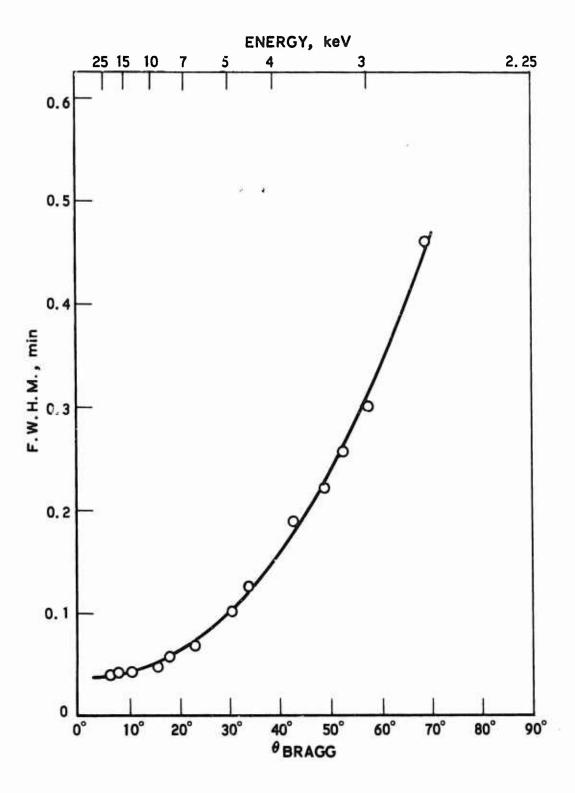


Figure 30. The F.W.H.M. of (1120) quartz. Data are reported by Parratt (15).

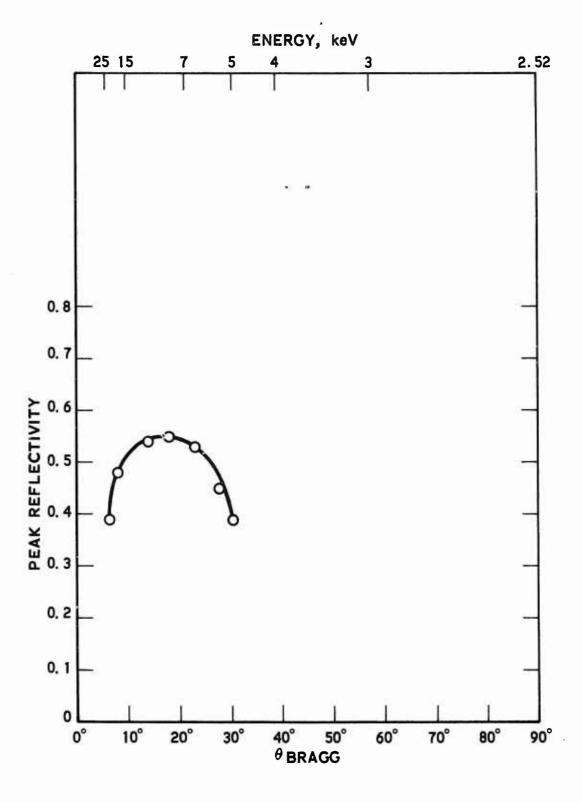


Figure 31. The peak reflectivity of (1120) quartz. Data are reported by Brogren (10).

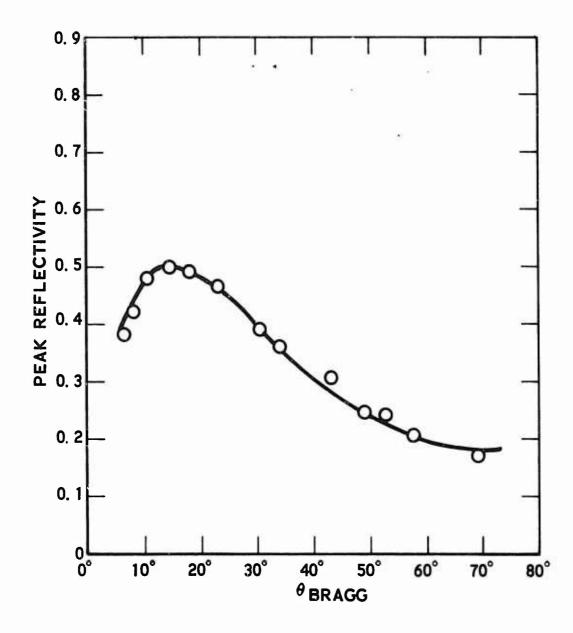


Figure 32. The peak reflectivity of (11 $\bar{2}0$ ) quartz. The data are reported by Parratt (15).

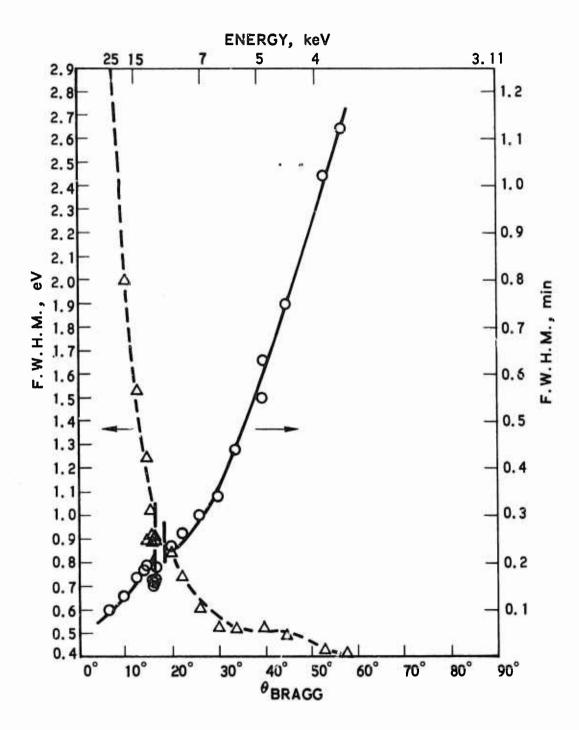


Figure 33. The F.W.H.M. of (220) Germanium. Solid line (F.W.H.M.  $\times \sqrt{2}$ ) in minutes (right-hand scale); dashed line in eV (left-hand scale). The data are reported by Brogren et al<sup>(12)</sup>.

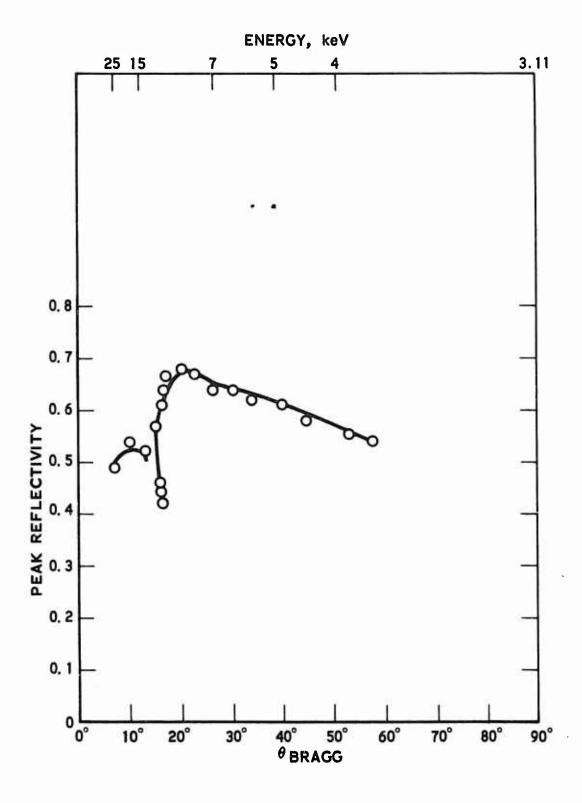


Figure 34. The peak reflectivity of (220) Germanium. The data are reported by Brogren et al<sup>(12)</sup>.

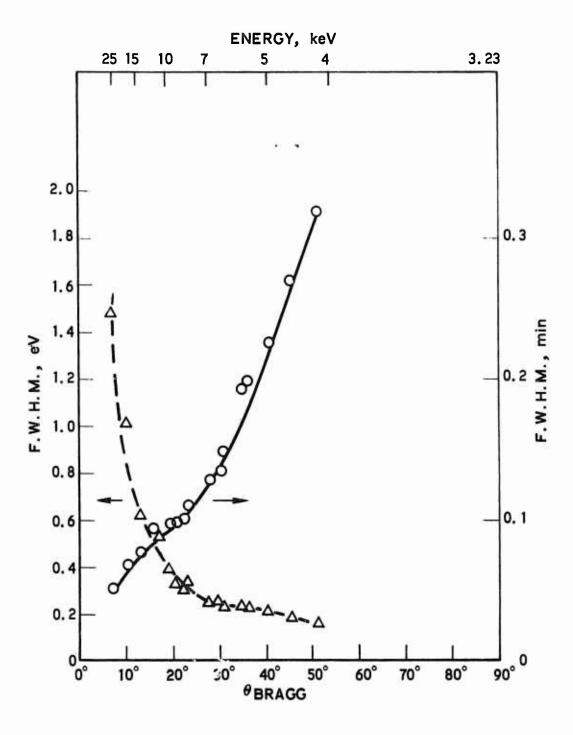


Figure 35.  $\sqrt{2}$  × F.W.H.M. of (220) silicon reported by Brogren et al<sup>(13)</sup>.

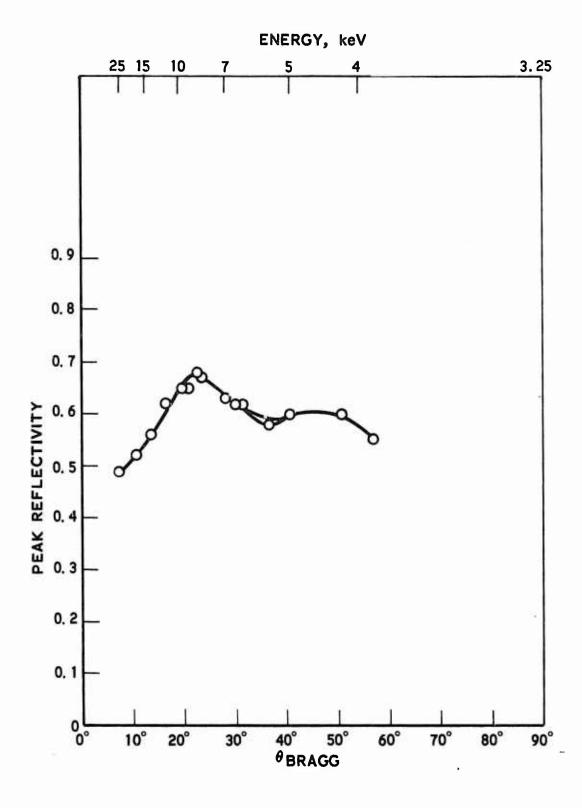


Figure 36. The peak reflectivity of (220) silicon reported by Brogren et al (13).

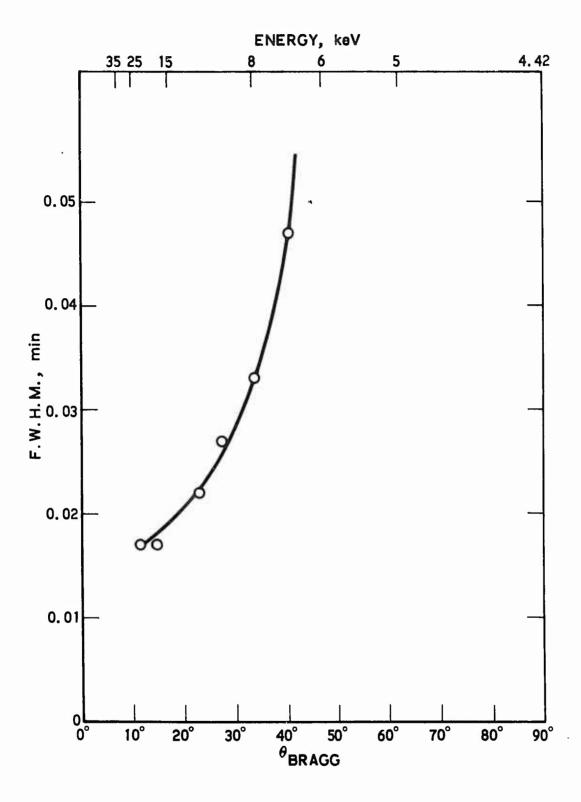


Figure 37.  $\sqrt{2} \times \text{F.W.H.M.}$  of  $(20\bar{2}\bar{3})$  quartz in minutes reported by Adell et al<sup>(8)</sup>.

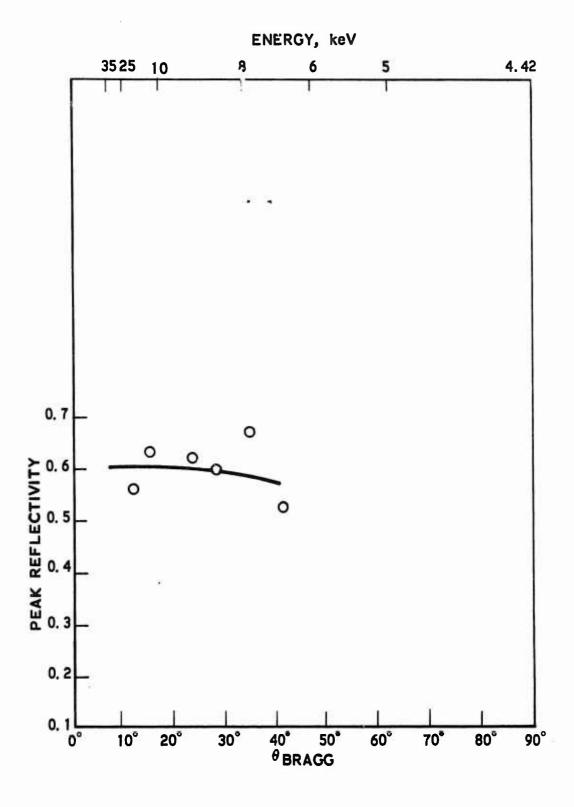


Figure 38. The peak reflectivity of (2023) quartz reported by Adell et al (8).

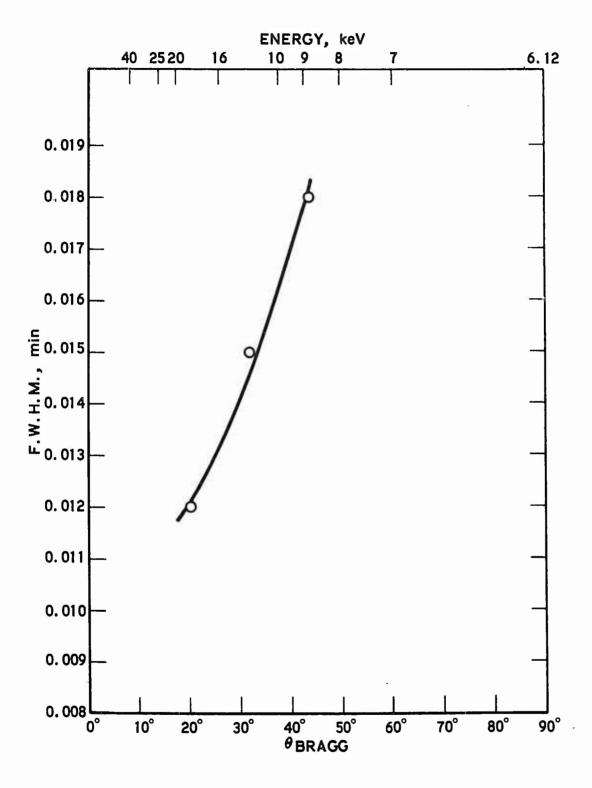


Figure 39. F.W.H.M.  $\times \sqrt{2}$  of (2243) quartz in minutes reported by Adell et al<sup>(8)</sup>.

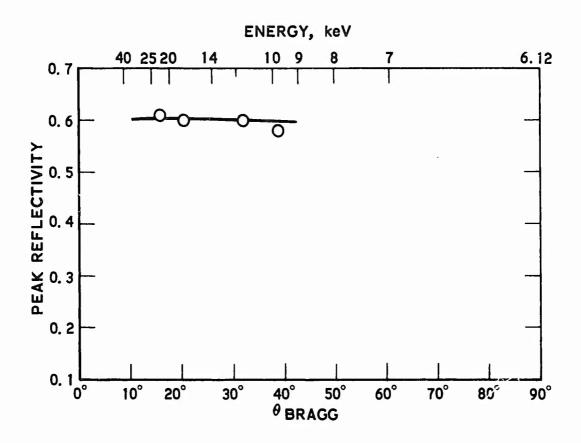


Figure 40. The peak reflectivity of (2243) quartz reported by Adell et al(8).

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# PART III. MULTI-PURPOSE TRIPLE CRYSTAL SPECTROMETER INTRODUCTION

In this third part of this report, a triple x-ray crystal spectrometer is described. There exists a considerable literature on the alignment and the theory of double crystal spectrometers, but little information on the alignment and theory of triple crystal spectrometers is available. It is, however, worthwhile to mention a useful graphical method introduced by DuMond. The method is simple and permits the definition, with some degree of accuracy, of the passband and the efficiency of a multi-crystal spectrometer. This approach to the understanding of a triple crystal spectrometer is considerably easier for the beginner than an approach utilizing analytic functions at the outset.

The method basically consists in the construction of a transparency for each crystal and a way to superimpose these transparencies. The transparency consists of a line described by the Bragg equation  $2d \sin \theta = n\lambda$ . The line thickness is proportional to the F. W. H. M. of the crystal rocking curve at a given wavelength and the line darkness is proportional to the peak reflectivity for the same wavelength. The transparencies of two crystals overlap in such a way that the angle axis is consistent in the parallel position (1-1) the angles increasing in the same direction, while in the antiparallel position they increase in opposite directions. In both cases, the distance between the origins of the two transparencies is equal to the dihedral angle between the crystals. In playing with these transparencies, it is easy to see some of the properties of a multi-crystal spectrometer.

#### CONSTRUCTION OF A MULTI-CRYSTAL SPECTROMETER

The spectrometer described below is the triple crystal spectrometer built for high resolution measurements making use of commercially available angular orientation devices. It can be used for a number of applications. Fig. 41 is the sideview of the spectrometer without the x-ray tube.

The chassis consists of an aluminum ( $40 \times 40 \times 1.5$  in.) plate, P<sub>4</sub>, with two axes  $A_1$ ,  $A_2$  attached on. The arm  $Ar_1$ , which rotate around axis  $A_1$ , supports the x-ray tube; the arm Ar<sub>2</sub> supports the second crystal, the axis for the third crystal and the stepping system. The arm's angular position is defined by the verniers  $V_{1.1}$ ,  $V_{2.1}$ . The  $A_{1.1}$  and  $A_{2.1}$  supports of the first and second crystal rotate inside the axes of A<sub>1</sub> and A<sub>2</sub>, respectively. The stainless steel plates P<sub>1.1</sub>, P<sub>2.1</sub>, the verniers V<sub>1.2</sub>, V<sub>2.2</sub> and long arms (for precise rotation) Ar<sub>1.1</sub>, Ar<sub>2.1</sub> are all screwed on to each of these axes  $(A_{1.1}, A_{2.1})$ . The plates support the Lansing translation stages L.T.S<sub>1</sub> and L. T. S2. The Lansing Angular Orientation Device, which is supported by the translation stages, has the crystal holders mounted on its center (not shown in the figure). The axis  $A_3$  is supported on the other end of arm  $Ar_2$ . The arm  $Ar_{3.1}$  which is on the  $A_3$  axis supports the detector D. The arm  $Ar_{3.2}$ , a long arm for precise rotation, and the vernier  $V_{3.1}$  are also attached to  $A_3$ . Inside the  $A_3$  axis, the  $A_3$  axis has an assembly similar to that above the other axes A1 and A2, i.e., the plate P3.1, the Lansing translation stage L.T.S3, the Lansing Orientation Device L.A.O.D3, the vernier  $V_{3.2}$ , and the arm  $Ar_{3.3}$  are all attached to the  $A_{3.1}$  axes. Fig. 42 is a view from the top of the arm Ar2 and shows the parts attached to it. The detector and the third crystal are rotated in a  $\theta\text{--}20$  motion with the help of the arms  $Ar_{3.2}$ ,  $Ar_{3.3}$  the micrometer  $M_4$  and the stepping motor S.M.<sub>1</sub>.

The Fig. 42 shows a top view of the arm Ar<sub>2</sub> with the assembly for the second and third crystal and also the micrometers and the additional arms.

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#### **AFPLICATIONS**

### High Resolution Spectrometer

The addition of a third crystal to a double crystal spectrometer mainly increases the dispersion and improves resolution to some extent, specifically in the tails of emission lines. However, the instrument has been used thus far as a double crystal spectrometer in the study of the spectra of scattered radiation. Using a set of two perfect crystals (333) planes a resolution of 25000 has been observed. Most of the measurements were carried out using a set of cleaved calcite crystal with a resolution of 5000. The sample under investigation was placed in the first crystal holder which was especially to shield the primary beam.

### X-Ray Topography

The system is ideal for accurate topographical work. The crystal under investigation is placed in the third crystal position with the first two crystals functioning as monochromator and collimators. A motor attached on micrometer  $M_{3,\,1}$  provides the crystal translation necessary to obtain a scanning topograph. For an oscillating topograph, the oscillation is provided by the third crystal fine rotation system and the step Motor S. M.  $_4$ .

### Other Uses

A number of measurements can be carried out using the system and supporting the crystal sample in the second crystal holder. Such measurements are: the refractive index, the phonon distribution, Brillouin scattering.

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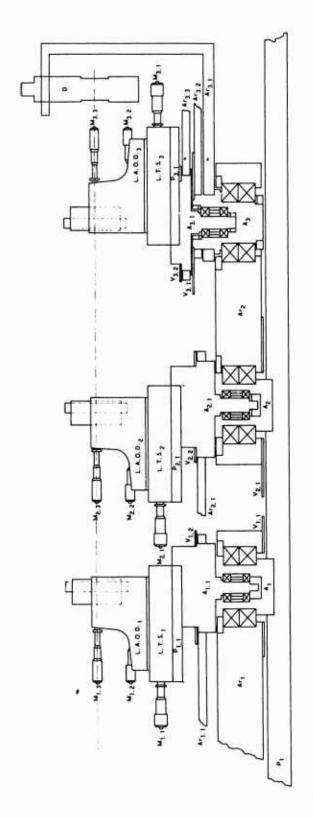


Figure 41. Sideview of the Triple Crystal Multi-Purpose Spectrometer

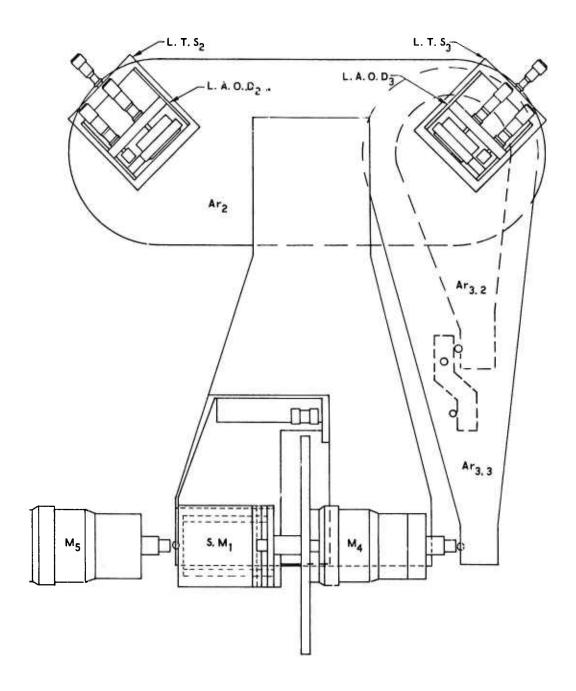


Figure 42. Top View of Arm Ar<sub>2</sub>